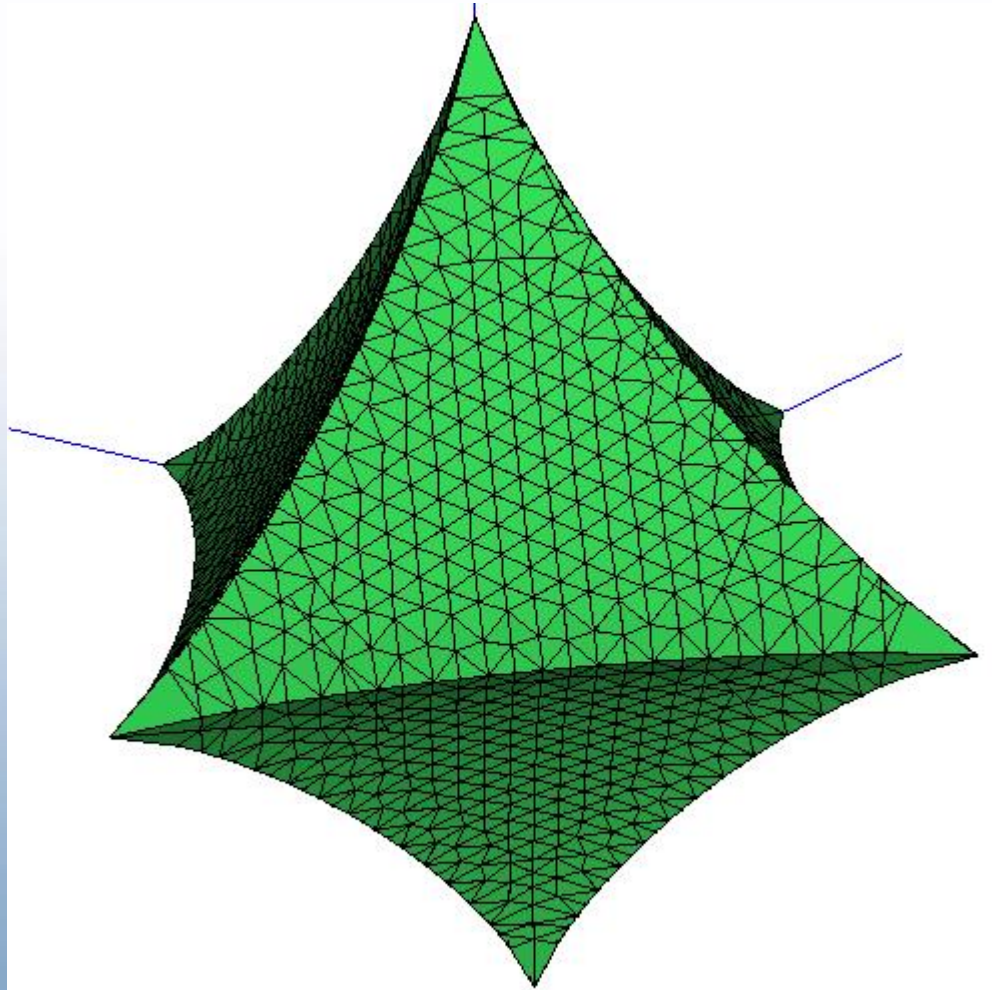




HyperFun Primitives



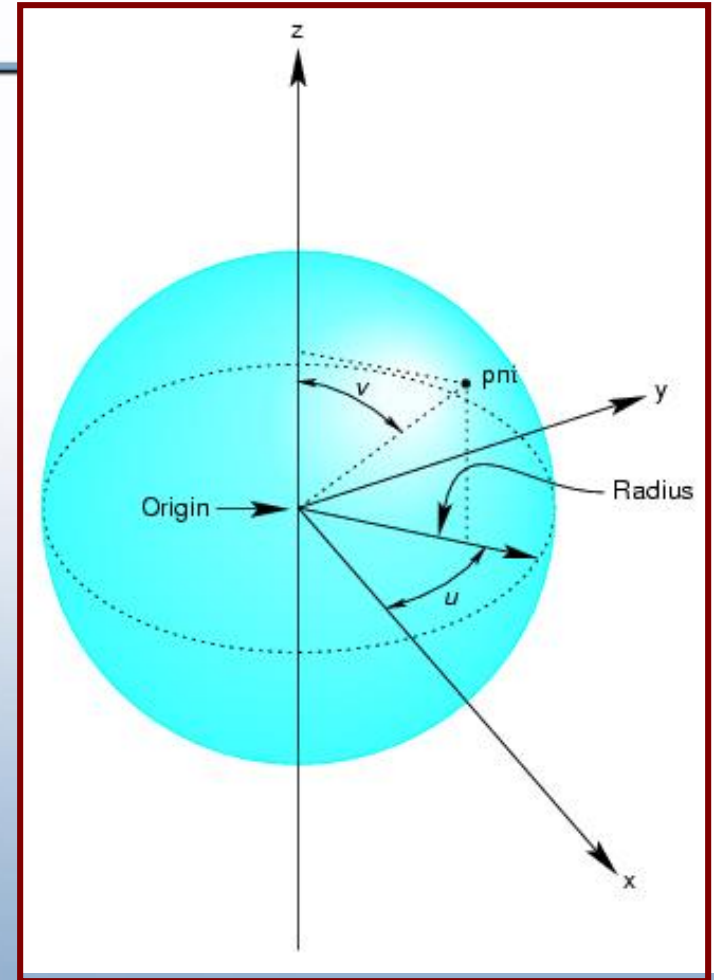


Solid Ball

Solid ball: $R^2 - x^2 - y^2 - z^2 \geq 0$

We can model a primitive in HyperFun by typing the analytical expression of its defining function:

```
Ball = R^2 - x[1]^2 - x[2]^2 - x[3]^2;
```





HyperFun: FRep Library

HyperFun has FRep library of predefined geometric objects or **primitives**, and predefined transformations of objects or **operations**. They are used in the model in two basic formats:

- ❖ for those, which require point coordinates **\mathbf{x}** as input,

hf<Name>(x, <parameters>)

- ❖ or simply

hf<Name>(<parameters>)

for others, where <parameters> is comma separated list of input parameters.



Primitives

Algebraic primitives: *hfSphere, hfEllipsoid, hfBlock, hfCylinder, hfEllCylinder, hfEllCone, hfTorus, hfSuperel.*

Skeletal objects: *hfBlobby, hfMetaball, hfSoft*

Convolution objects: *hfConvPoint, hfConvLine, hfConvArc, hfConvTriangle, hfConvCurve, hfConvMesh*

Procedural objects: *hfNoiseG*

Operations

hfScale, hfShift, hfRotate, hfTwist, hfStretch, hfTaper, hfBlendUni, hfBlendInt



Algebraic Surfaces

Surfaces with polynomial $f(x,y,z)$

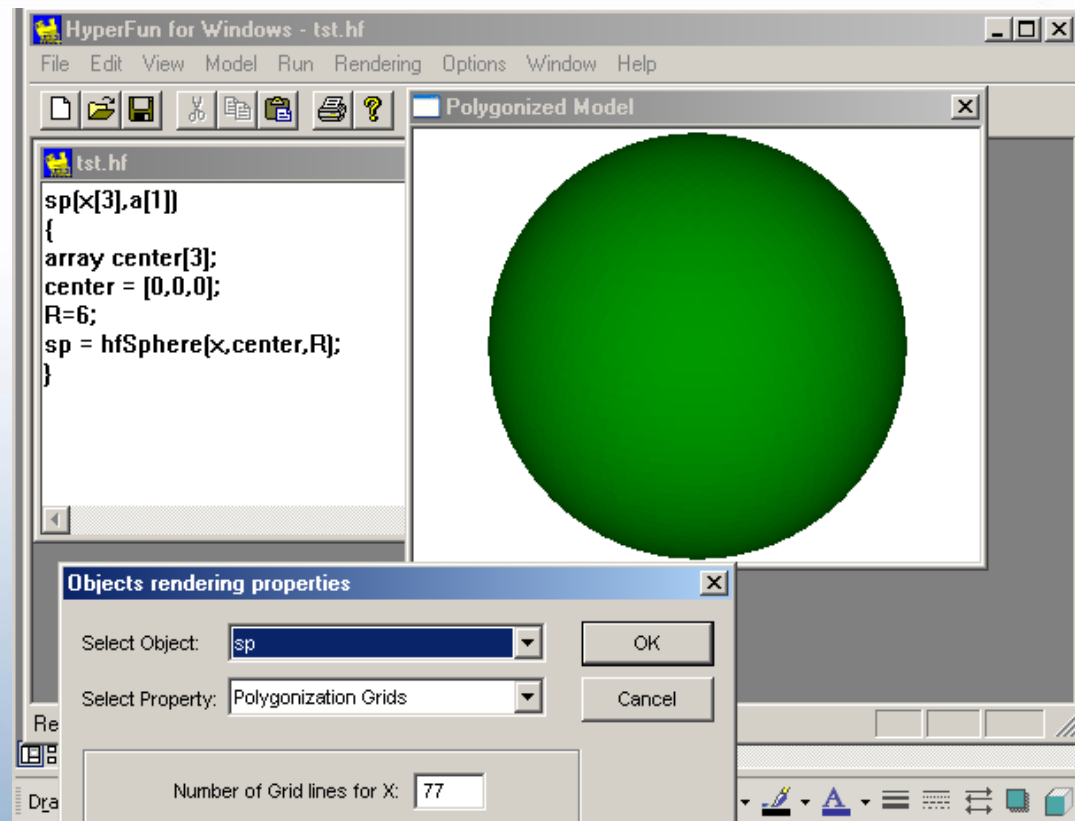
- Quadratic
 - Sphere
 - Ellipsoid
 - Cylinder
 - Cone
- ...
- Torus
- Superellipsoid



Library primitive: Sphere and Solid Ball

Sphere/ball of radius 6:

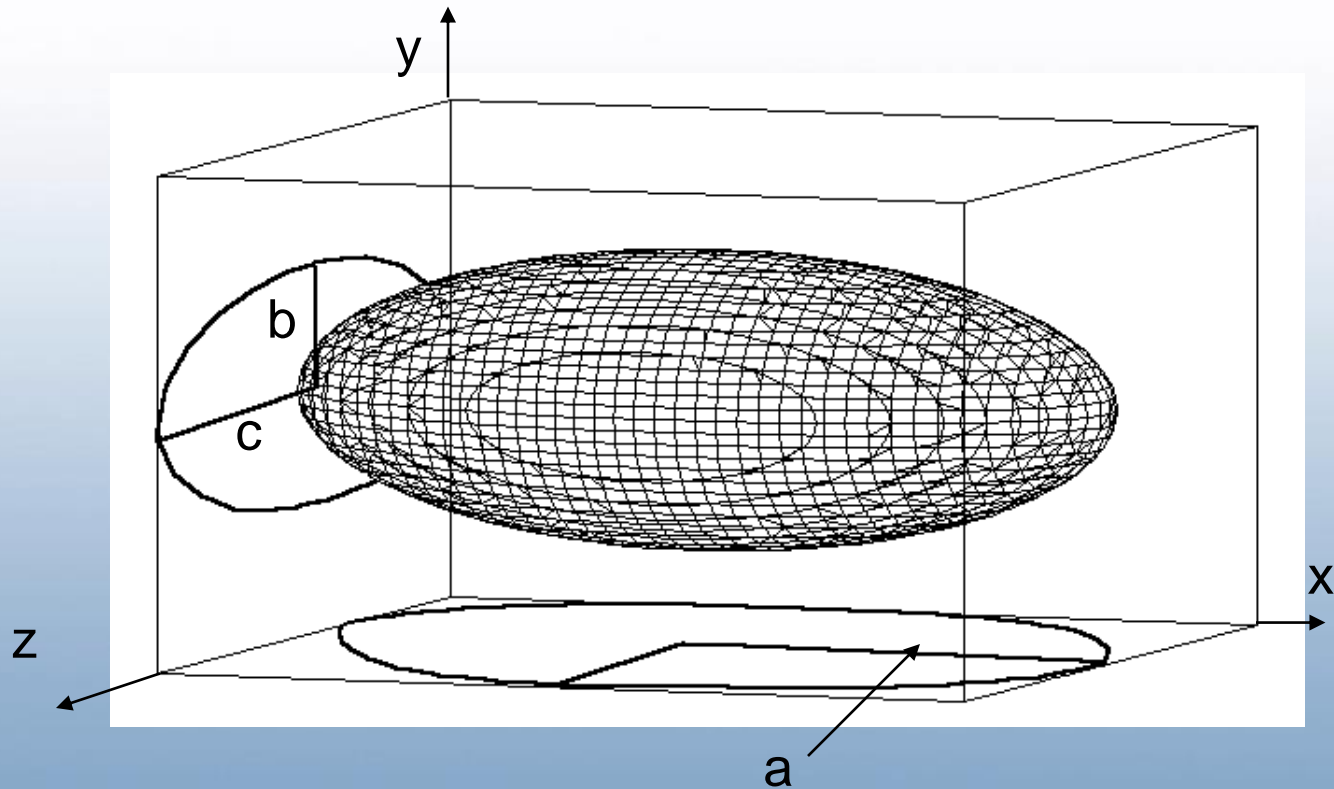
```
sp(x[3],a[1])  
{  
  array center[3];  
  center = [0,0,0];  
  R=6;  
  sp = hfSphere(x,center,R) ;  
}
```





Ellipsoid

$$F(x,y,z) = 1 - (x/a)^2 - (y/b)^2 - (z/c)^2$$

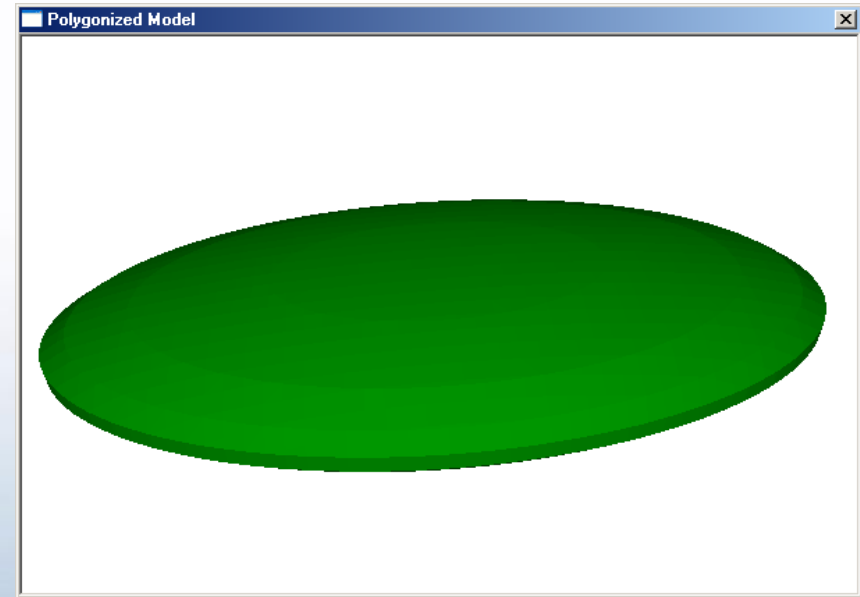




Library primitive: Ellipsoid

Ellipsoid with half-axes 6,3,1:

```
e1(x[3],a[1])  
{  
  array center[3];  
  center = [0,0,0];  
  e1 = hfEllipsoid(x,center,6,3,1);  
}
```

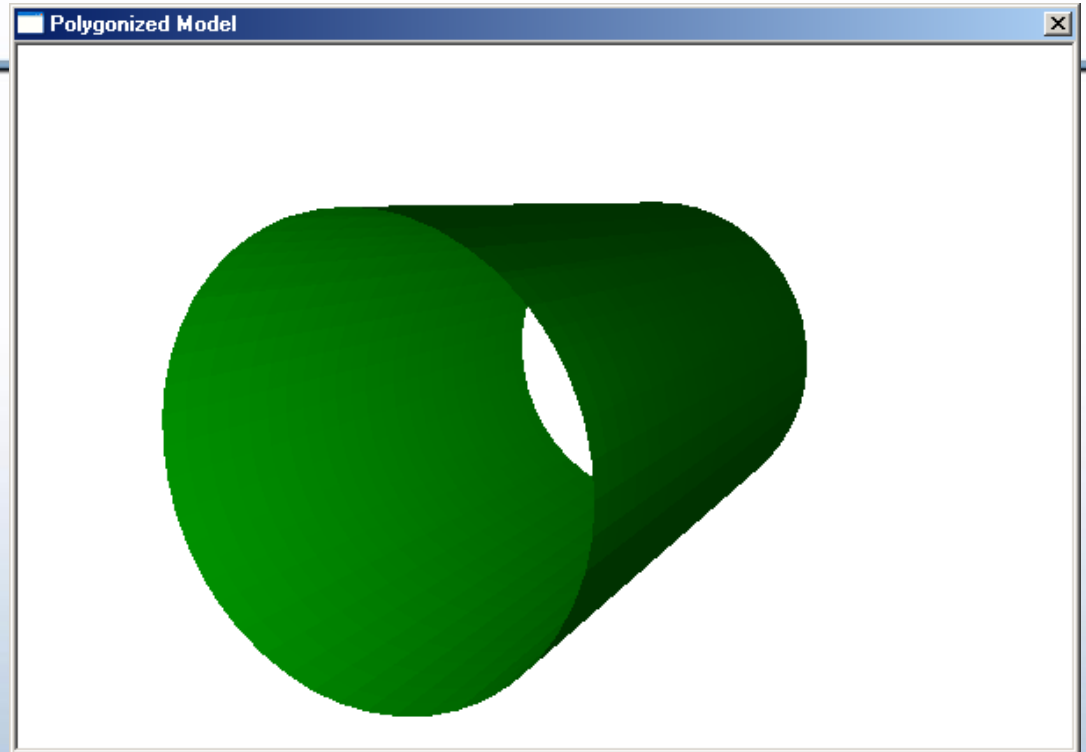




Library primitive: Cylinder

Cylinder with axis Z
and radius 6:

```
cyl(x[3],a[1])  
{  
  array center[3];  
  center = [0,0,0];  
  cyl = hfCylinderZ(x,center,6);  
}
```



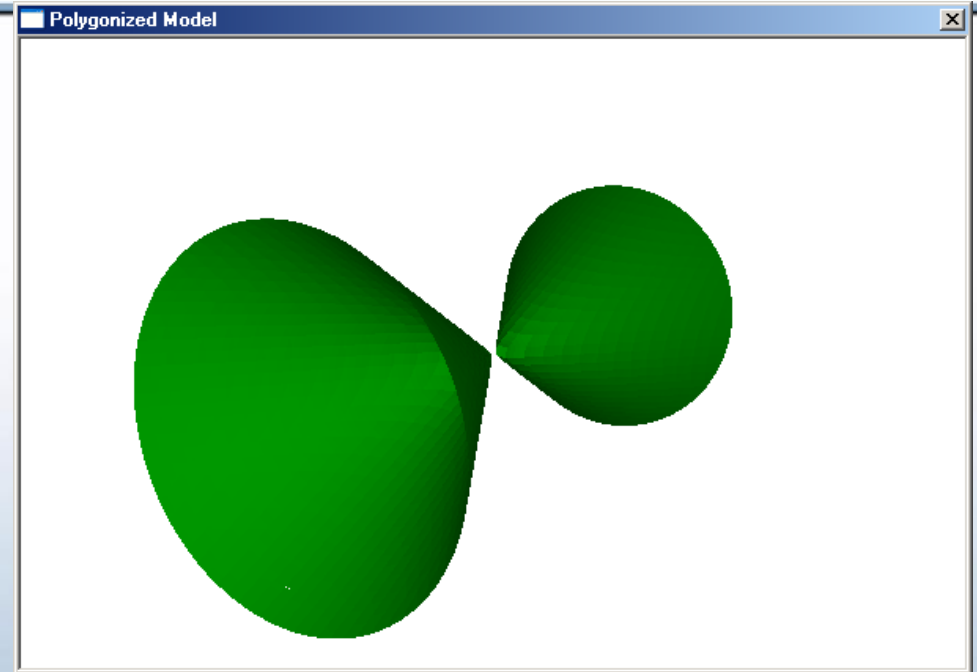
Note: the primitive is infinite solid, the surface is cut on both ends for visualization



Library primitive: Cone

Cone with axis Z and
radius 0.5 at height 1:

```
cone(x[3], a[1])  
{  
  array center[3];  
  center = [0,0,0];  
  cone = hfConeZ(x, center, 0.5);  
}
```

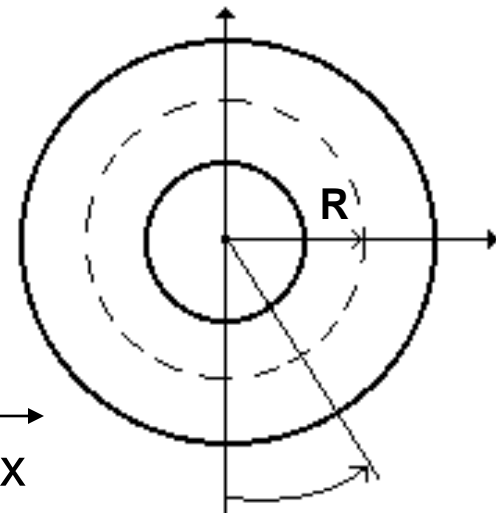
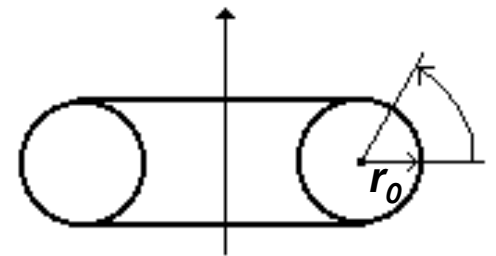
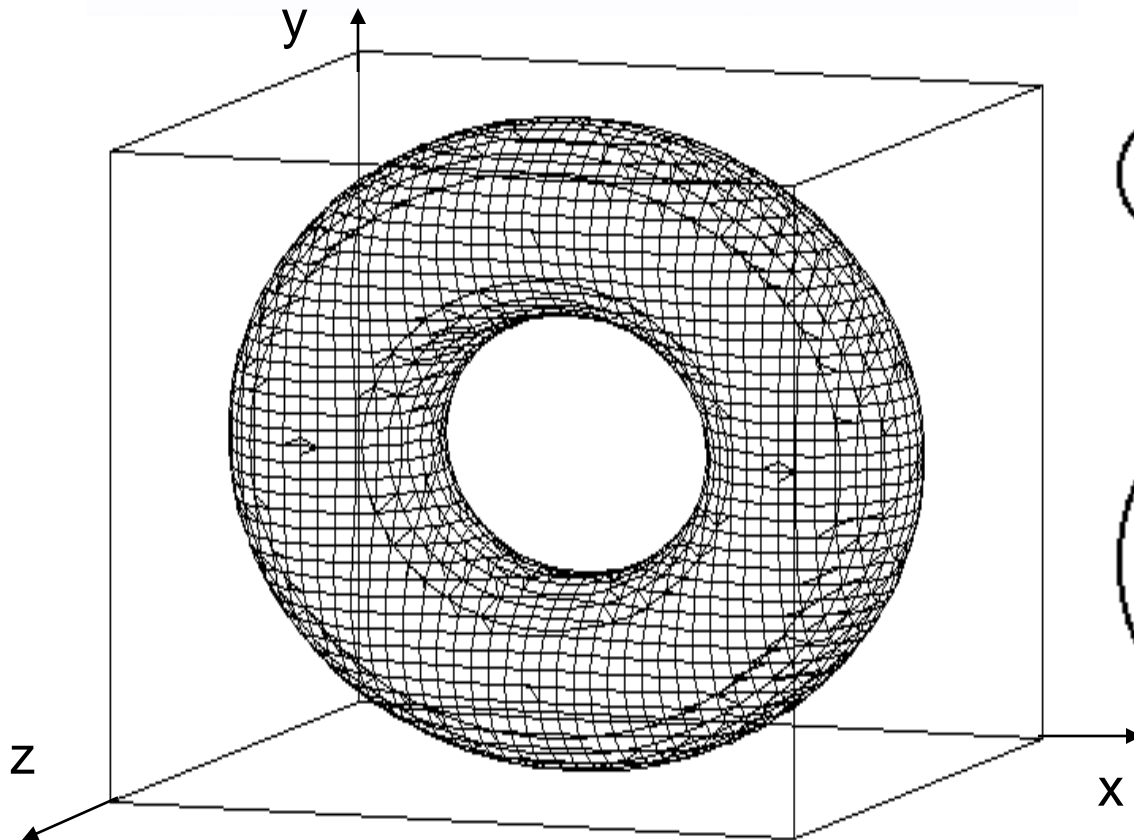


Note: the primitive is infinite solid with both branches of the cone present, the surface is cut on both ends for visualization



Torus

$$F(x,y,z) = r_0^2 - x^2 - y^2 - z^2 - R^2 + 2R \sqrt{x^2 + y^2}$$

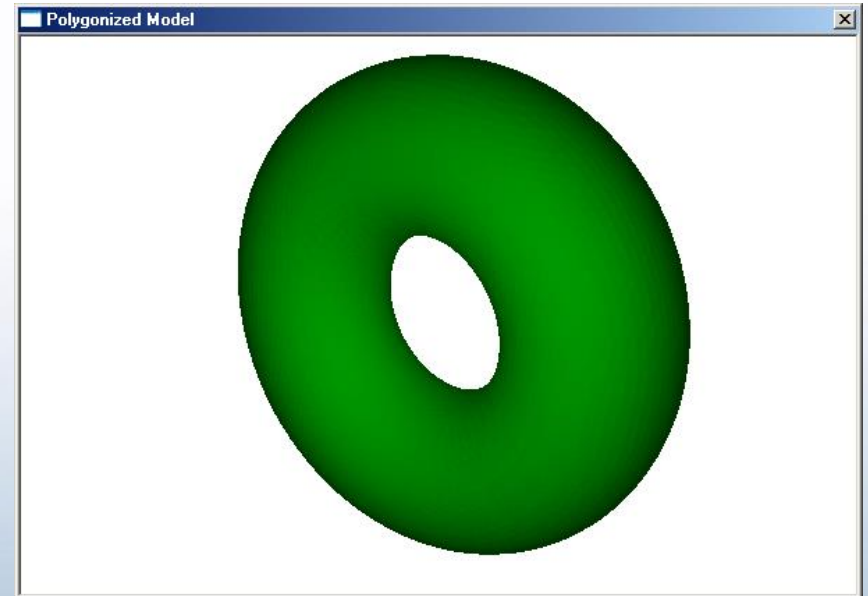




Library primitive: Torus

Torus with axis Z,
radii $R=6$ and $r_0=3$:

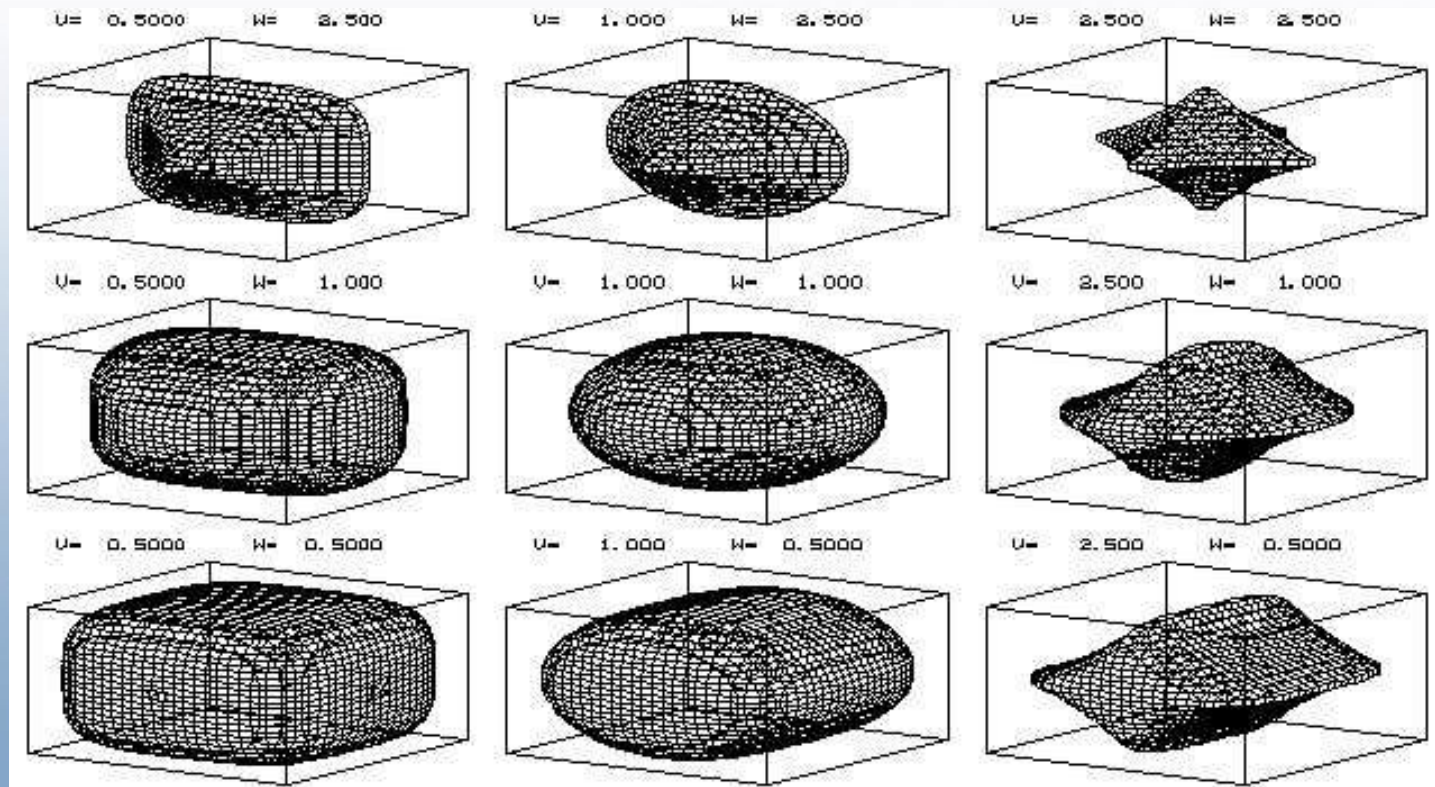
```
torus (x[3] , a[1])  
{  
  array center[3];  
  center = [0,0,0];  
  R=6;  
  r0=3;  
  torus =  
    hfTorusZ (x, center, R, r0) ;  
}
```





Superellipsoids

$$f(x, y, z) = 1 - \left[\left(\frac{x}{r_x} \right)^{\frac{2}{s_2}} + \left(\frac{y}{r_y} \right)^{\frac{2}{s_2}} \right]^{\frac{s_2}{s_1}} - \left(\frac{z}{r_z} \right)^{\frac{2}{s_1}}$$

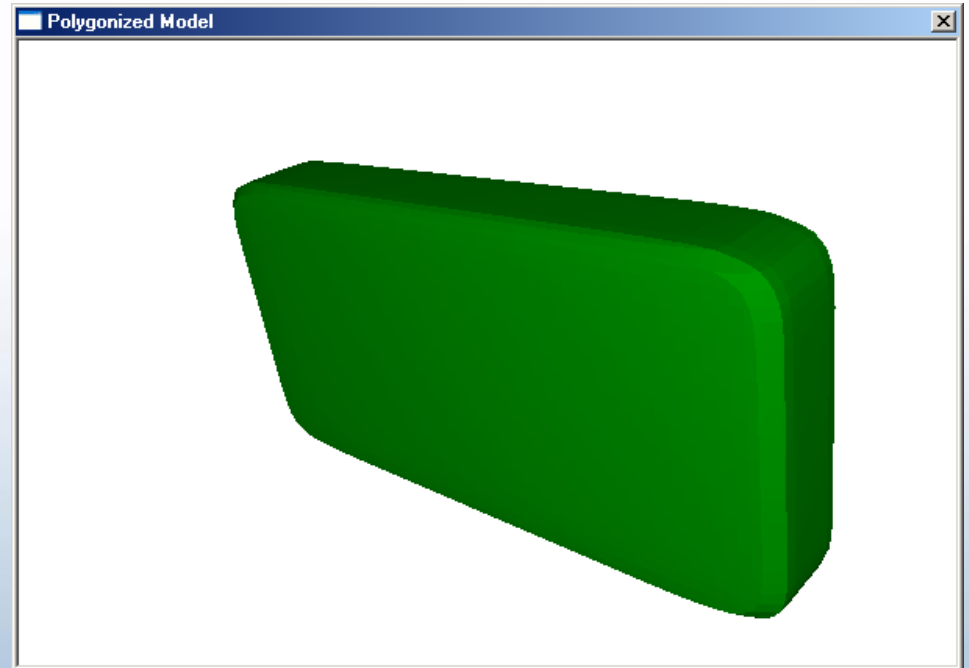




Library primitive: Superellipsoid

Superellipsoid with
parameters $s_1 = s_2 = 0.2$

```
super(x[3], a[1])  
{  
  array center[3];  
  center = [0,0,0];  
  super =  
    hfSuperell(x, center, 6, 3, 1, 0.2, 0.2);  
}
```





Superellipsoids

